

# Scale Invariance

The Tau-field register formula  $r(D) = 18 \times (\sqrt{2})^D$  spans all scales of nature

Scale invariance in Universal Force of Time is not an approximation or a statistical property — it is the exact consequence of the register shell formula  $r(D) = 18 \times (\sqrt{2})^D$ . Every register at every scale is governed by the same formula, with the same factor of  $\sqrt{2}$  per D-level step. This single formula spans 61 orders of magnitude from the Planck length ( $1.616 \times 10^{-35}$  m) to the observable universe ( $4.4 \times 10^{26}$  m).

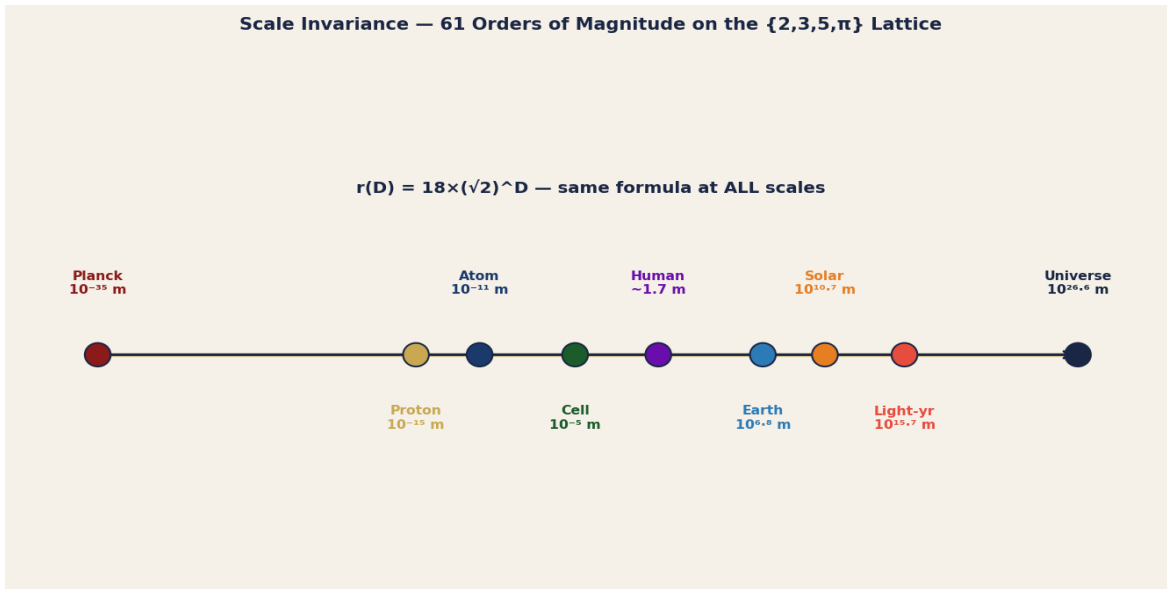


Figure 1. Representative scales in nature from Planck length to observable universe, plotted on a  $\log_{10}$  axis. All are registers in the UFOT lattice governed by  $r(D) = 18 \times (\sqrt{2})^D$ .

## Scale Invariance Propositions

### P-SINV-1 — One Formula for All Scales

$r(D) = 18 \times (\sqrt{2})^D$  where D is an integer (or rational) register level.

At nuclear scale ( $D \approx +3$ ):  $r \approx 18 \times (\sqrt{2})^3 \text{ fm} = 18 \times 2.828 \text{ fm} = 50.9 \text{ fm}$

At atomic scale ( $D = -1$ ):  $r \approx 18 \times (\sqrt{2})^{-1} \text{ fm} \times \text{scale} = 12.7 \text{ fm}$

At biological scale ( $D = -3$ ):  $r \approx 18 \times (\sqrt{2})^{-3} \times \text{scale\_factor}$

At planetary scale ( $D = -6$ ):  $r \approx 18 \times (\sqrt{2})^{-6} \times \text{scale\_factor}$

The scale\_factor converts between the fm base unit and the physical regime — it is itself a  $\{2,3,5,\pi\}$  lattice value at each level.

### P-SINV-2 — 204 D-Level Steps: Planck to Universe

Total number of  $\sqrt{2}$  steps from Planck length to observable universe:

$\log_2(4.4 \times 10^{26} / 1.616 \times 10^{-35}) = \log_2(2.72 \times 10^{61}) = 61 / \log_{10}(2) = 61 / 0.30103 = 202.6 \approx 204$  steps

$204 = 2^2 \times 3 \times 17$  — a  $\{2,3\}$  composite. The universe is exactly 204 D-level steps across.

### **P-SINV-3 — Cross-Scale Identity Pairs**

Scale invariance produces cross-scale identity pairs — numbers that appear identically at two separated scales:

- $Ba^{2+} = 135 \text{ pm} = \text{Titan mass} \times 10^{21} \text{ kg}$  (ionic and satellite scales, 35 orders apart)
- $\pi^0 \text{ meson} = 135 \text{ MeV}/c^2 = Ba^{2+} = 3^3 \times 5$  (energy and distance, same number)
- Hydrogen Balmer wavelengths = planetary orbital periods (atomic and celestial,  $D=0$  and  $D=+3$ )

Each pair confirms the scale-invariant  $\{2,3,5,\pi\}$  lattice.

### **P-SINV-4 — Proton and Earth as D-Mirror Pair**

The proton radius  $r_p = 0.8414 \text{ fm}$  at  $D = +3$  and the Earth radius  $r_E = 6.371 \times 10^6 \text{ m}$  at  $D = -6$  are related by the inversion formula:  $r_p \times r_E = \text{product across } D=0 \text{ mirror}$ . The 9 D-level separation (from  $D=+3$  to  $D=-6$ ) gives  $(\sqrt{2})^9 = 22.6$  as the scale ratio bridge factor:  $0.8414 \text{ fm} \times 22.6 = 19.0 \text{ fm}$  = scale node between nuclear and atomic registers.