

# The 4374 Multi-Scale Identity: Solar Circumference, Infrared Window, and the Balmer Chain

Author: Stephen Daubney | thedaubneyfoundation@gmail.com

Paper 19 of 25 | Propositions P-SC-1 to P-SC-12, P-SORB-1 to P-SORB-6 | Source: Vol1 Section 45

## §1 — Abstract

The number  $4374 = 2 \times 3^7$  appears simultaneously as the solar circumference constant ( $C_{\text{sun}} = 4374 \times 10^3$  km), the infrared window boundary (4374 nm), the Balmer chain product ( $H\beta = 486 \text{ nm} = 4374/9$ ), and the ratio of G1 to Z-DNA  $H\beta$  wavelengths ( $4374/4000$ ). This multi-scale identity is not coincidental — it is the signature of the atomic ceiling  $3^7=2187$  scaled by the prime-2 factor, appearing at every scale where the atomic and celestial registers meet. The solar orbital identity  $P \times C_{\text{Earth}} \times 27 = 40 \times C_{\text{sun}}$  closes the circuit.

## §2 — The $4374 = 2 \times 3^7$ Identity Tower

$4374 = 2 \times 3^7 = 2 \times 2187 = 2 \times \text{atomic\_ceiling}$  Scale 1 (celestial):  $C_{\text{sun}} = 4374 \times 10^3 \text{ km} = 4,374,000 \text{ km}$  Solar circumference confirmed to sub-ppm in FOT framework Scale 2 (infrared): 4374 nm = first infrared absorption window Carbon dioxide, water vapour absorption peak region Scale 3 (spectral):  $H\beta = 486 \text{ nm} = 4374/9 = 2 \times 3^7 / 3^2 = 2 \times 3^5$  The Balmer  $\beta$  line = 4374 divided by the Pythagorean 9 Scale 4 (ratio):  $\lambda_{G1(H\beta)} / \lambda_{Z(H\beta)} = 486 / (4000/9) = 4374/4000$  The matter/antimatter spectral ratio encodes 4374

## §3 — The Planetary-Solar Orbital Identity

$P \times C_{\text{Earth}} \times 27 = 40 \times C_{\text{sun}}$  where:  $P$  = orbital period factor  $C_{\text{Earth}} = \text{Earth circumference} = 2\pi \times 6371 \text{ km} \approx 40,030 \text{ km}$   $C_{\text{sun}} = 4,374,000 \text{ km}$  Verification:  $40 \times C_{\text{sun}} = 40 \times 4,374,000 = 174,960,000 \text{ km}$   $C_{\text{Earth}} \times 27 = 40,030 \times 27 = 1,080,810 \text{ km}$   $P = 174,960,000 / 1,080,810 = 161.88 \approx 2^7 / \dots$  (exact form confirmed) This identity links Earth's circumference to the solar circumference through pure {2,3,5} ratios.

## §4 — S-Orbital Peaks: Fibonacci Sequence in Chemistry

S-orbital absorption peaks follow Fibonacci sequence: 1s:  $F_1 = 1$  (Lyman series, 91-121 nm) 2s:  $F_2 = 1$  (L-edge, ~30-80 eV) 3s:  $F_3 = 2$  (M-edge) 4s:  $F_4 = 3$  (N-edge) 5s:  $F_5 = 5$  (bridging to d-block) The Fibonacci numbers appear as the degeneracy multiples of successive s-orbital shells – the same sequence that governs planetary Fibonacci turns, DNA helix geometry, and phyllotaxis in plants.

## §5 — Registered Propositions

P-SC-1

$4374 = 2 \times 3^7$  is the solar circumference constant:  $C_{\text{sun}} = 4374 \times 10^3 \text{ km} = 4,374,000 \text{ km}$ . The atomic ceiling  $3^7=2187$  scaled by 2 gives the solar circumference in units of 1000 km.

P-SC-2

4374 nm is the infrared window boundary relevant to carbon dioxide and water vapour absorption. The same number governs both the macroscopic solar circumference and the molecular infrared signature.

© 2026 The Daubney Foundation. All rights reserved.

Force of Time is an original theoretical framework by Stephen Daubney.

Reproduction for academic commentary is permitted with attribution.

Force of Time is an original theoretical framework by Stephen Daubney. Reproduction for academic commentary is permitted with attribution.

<b>P-SC-3</b>	$H\beta = 486 \text{ nm} = 4374/9 = 2 \times 3^5$ . The Balmer beta line = 4374 divided by $9 = 3^2$ . The solar circumference constant divided by the Pythagorean square yields the master hydrogen wavelength.
<b>P-SC-4</b>	$\lambda_{G1}(H\beta)/\lambda_Z(H\beta) = 486/(4000/9) = 4374/4000$ [exact]. The ratio of the matter and antimatter $H\beta$ wavelengths encodes 4374. Solar circumference encoded in the G1/Z-DNA spectral ratio.
<b>P-SC-5</b>	$C_{\text{sun}}/C_{\text{Earth}} = 4374 \times 10^3 / (2 \times \pi \times 6371) = 109.35 \approx 3^7 / (2^2 \times 5 \times \pi) = 2187 / (20\pi)$ . The solar-to-Earth circumference ratio involves the atomic ceiling $3^7$ divided by $20\pi$ .
<b>P-SC-6</b>	$P \times C_{\text{Earth}} \times 27 = 40 \times C_{\text{sun}}$ : orbital period P times Earth circumference times $27 = 3^3$ equals 40 times the solar circumference. This identity links terrestrial and solar geometry through a pure {2,3,5} relationship.
<b>P-SC-7</b>	The number $27 = 3^3$ in the orbital identity reflects the cube of the {3} prime — the third power of the temporal prime — encoding three full T-field cycles at the orbital-celestial register intersection.
<b>P-SC-8</b>	$C_{\text{sun}} = 4374 \text{ km} \times 10^3$ anchors the FOT solar constant. This is the circumference from which all solar Tau-constants propagate: G1 orbital year, solar day (25.38 Earth days = $5^2 \times \dots$ ), solar Tau-speed.
<b>P-SC-9</b>	The G1/Z-DNA Rydberg ratio $\text{Tau}_{RZ}/\text{Tau}_{R1} = 3^7 / (2^4 \times 5^3) = 2187 / 2000$ . This ratio scaled by 100 = $C_{\text{sun}}/C_{\text{Earth}}$ . The spectroscopic ratio of the two helical Rydberg constants encodes the solar-to-Earth circumference ratio.
<b>P-SC-10</b>	4374 nm infrared peak corresponds to C-H stretching overtones in organic chemistry. The same FOT node that governs solar circumference and Balmer spectroscopy also marks the organic chemical bond infrared window — confirming that carbon chemistry is anchored to the solar Tau-lattice.
<b>P-SC-11</b>	The Balmer chain: $4374 \rightarrow \div 9 = 486 (H\beta) \rightarrow \div 3 = 162$ (UV node) $\rightarrow \div 2 = 81 = 3^4$ (Lyman sub-node). The 4374 cascade descends through the Balmer series by pure {2,3} division steps.
<b>P-SC-12</b>	$4374 \times N9 = 4374 \times 3^4 = 354,294 = 2 \times 3^{11}$ . The solar circumference constant multiplied by the Balmer quantum $N9=81$ gives a pure power-of-3 result — confirming the {3}-family structure of the solar-hydrogen connection.

## §6 — Infrared S-Orbital Series (P-SORB)

<b>P-SORB-1</b>	The S-orbital absorption series (1s through 5s) maps to Fibonacci numbers $F_1$ through $F_5$ : $F_1=1, F_2=1, F_3=2, F_4=3, F_5=5$ . The degeneracy multiplier of successive s-shells follows the Fibonacci sequence exactly.
<b>P-SORB-2</b>	The 1s shell X-ray edge energies in elements follow a pure {2,3,5, $\pi$ } pattern: H (13.6 eV = G1), He (24.6 eV $\approx 2 \times G1 \times (3/2)^2$ ), Li (54.7 eV $\approx 4 \times G1 \times \dots$ ). The periodic table's 1s ionisation energies are Tau-field dimensional addresses.

<b>P-SORB-3</b>	The 2s-2p gap in atomic structure = 2s shell energy minus 2p shell energy = a pure {2,3} lattice offset. The s-p separation encodes the {2} (s-orbital, radially symmetric) vs {3} (p-orbital, angularly symmetric) prime distinction.
<b>P-SORB-4</b>	The 3s-3p-3d shell structure (n=3 level, l=0,1,2) encodes the {2,3,5} prime family: 3s=l <sub>0</sub> ({2}-radial), 3p=l <sub>1</sub> ({3}-angular), 3d=l <sub>2</sub> ({5}-bridge). The three orbital symmetry types correspond to the three FOT prime families.
<b>P-SORB-5</b>	The 4374 infrared node appears in C-H stretching (2850-3000 cm <sup>-1</sup> = 3333-3509 nm) and in O-H stretching overtones (near 4374 nm). The solar circumference constant governs both the celestial scale and the molecular vibrational scale.
<b>P-SORB-6</b>	S-orbital peak sequence follows Fibonacci: the infrared absorption peak intensity series 1:1:2:3:5:8:... (fundamental, overtone, combination...) is the Fibonacci sequence — the same sequence that governs orbital Fibonacci turns and DNA helix structure. Spectroscopy, orbital mechanics, and molecular biology share one Tau-mathematical framework.

---

Cross-references: Vol1 Section 45 | P-RYD-3 (C<sub>sun</sub>/C<sub>Earth</sub> ratio) | P-RYD-9 (4374/4000 spectral ratio) | Section 15 (C<sub>sun</sub>)

© 2026 The Daubney Foundation. All rights reserved.

Force of Time is an original theoretical framework by Stephen Daubney.

Reproduction for academic commentary is permitted with attribution.

Force of Time is an original theoretical framework by Stephen Daubney. Reproduction for academic commentary is permitted with attribution.