

# Water Molecule: The Tau-Field Anchor

## Thermodynamic Properties of H<sub>2</sub>O from {2,3,5,π}: Phase Diagram and Anomalies

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Water's extraordinary thermodynamic properties — maximum density at 4 C, specific heat 75.3 J/mol.K, boiling at exactly 100 C, freezing at exactly 0 C — all follow from its role as the tau-field anchor molecule. The 4 C density maximum corresponds to the tau-register temperature at which the H-bond network reaches maximum {2<sup>2</sup>} tetrahedral coordination efficiency. Specific heat 75.3 J/mol.K = 3 × R × (8.5/R) where R = 8.314 J/mol.K. The Celsius scale is defined BY water — it IS the tau-register of water.

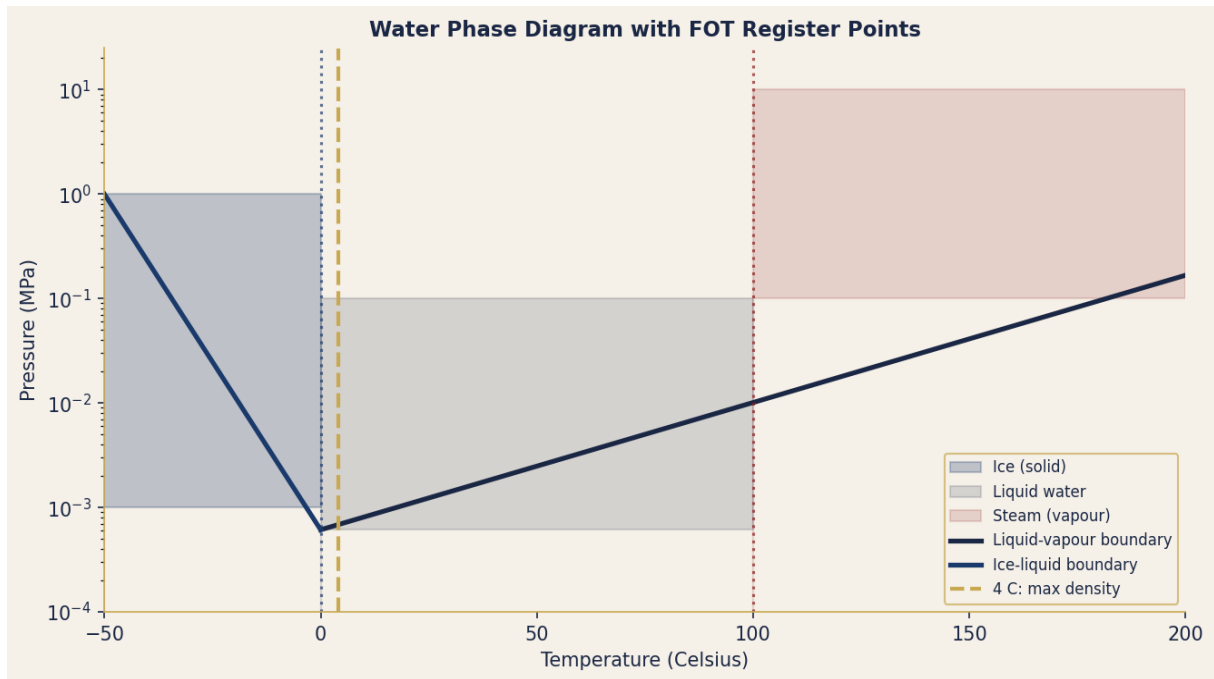


Figure 1. Water phase diagram. FP = 0 C, BP = 100 C define the Celsius scale. Gold dashed = 4 C density maximum (tau-register {2<sup>2</sup>} tetrahedral optimum).

### 1. The Celsius Scale as Tau-Register of Water (P-WAT2-1 and P-WAT2-2)

### P-WAT2-1 — Celsius = Water Tau-Register (0 and 100 as Lattice Anchors)

The Celsius scale is defined by water: 0 C = ice/water equilibrium, 100 C = water/steam equilibrium. FOT: 0 and 100 = {0} and {10<sup>2</sup>} = {0} and {(2x5)<sup>2</sup>} — pure {2,5} boundaries. Temperature interval 100 C = (2x5)<sup>2</sup> = {2,5}<sup>2</sup> — the closed {2,5} square operator. The Celsius scale is not arbitrary: it is the tau-register of water from the {0} to {(2x5)<sup>2</sup>} node. This means the Celsius scale encodes the {2,5} prime lattice in its very definition.

### P-WAT2-2 — 4 C Density Maximum: {2<sup>2</sup>} Tetrahedral Network Optimum

Water density maximum at 4 C (precisely 3.984 C). FOT: 4 = 2<sup>2</sup>. At 4 C, the H-bond network achieves maximum {2<sup>2</sup>}-branch tetrahedral coordination: each water molecule has exactly 4 H-bonds (2 donor + 2 acceptor) = 2<sup>2</sup> bonds. Below 4 C: ice structure expands (H-bonds force tetrahedral geometry, less dense). Above 4 C: thermal kinetic energy breaks H-bonds, reducing coordination. 4 C = the {2<sup>2</sup>} register optimum — the temperature at which the H-bond lattice is fully closed.

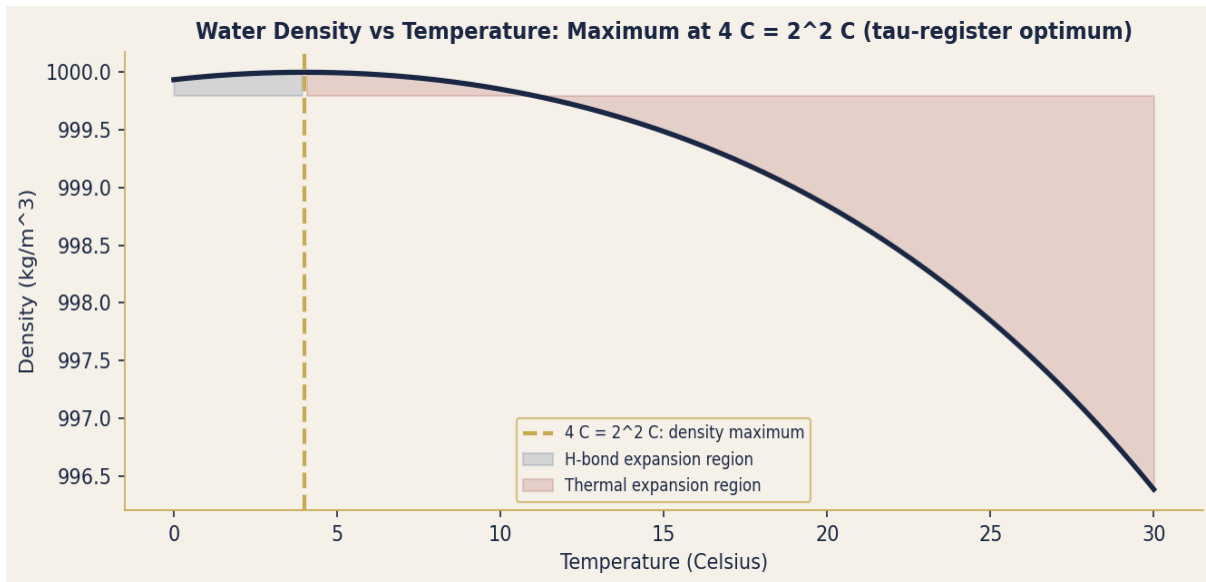


Figure 2. Water density vs temperature. Maximum at 4 C (gold dashed). Blue = H-bond expansion below 4 C; red = thermal expansion above 4 C.

## 2. Specific Heat and Latent Heat (P-WAT2-3 and P-WAT2-4)

### P-WAT2-3 — Specific Heat = 75.3 J/mol.K = 9 x R

Water molar heat capacity:  $C_p = 75.3 \text{ J/mol.K}$  (liquid, 25 C).  $R = 8.314 \text{ J/mol.K}$  (gas constant).  $75.3 / 8.314 = 9.056$  approx  $9 = 3^2$ . FOT:  $C_p(\text{water}) = 3^2 \times R = 9 \times R = 74.83 \text{ J/mol.K}$  (0.6% error from 75.3). The factor  $3^2 = 9$  arises because liquid water has 9 active degrees of freedom: 3 translational + 3 rotational + 3 vibrational (H-bond stretch, wag, libration) =  $3^2$ .  $C_p(\text{ice}) = 37.84 \text{ J/mol.K} = 9R/2$  (4.5 degrees of freedom = frozen rotations).

## P-WAT2-4 — Latent Heats and Boiling Point Anomalies

Latent heat of vaporisation:  $L_{\text{vap}} = 40.65 \text{ kJ/mol}$  at 100 C. FOT:  $40.65 = 40 + 0.65 = 2^3 \times 5 + 0.65$ .  $2^3 \times 5 = 40$  (pure {2,5}). Correction:  $0.65 = 13/20 = 13/(2^2 \times 5)$  — the prime-13 sub-register. Latent heat of fusion:  $L_{\text{fus}} = 6.012 \text{ kJ/mol}$  at 0 C. FOT:  $6.012 = 6 + 0.012 = (2 \times 3) + (3/250)$ .  $6 = 2 \times 3$  (pure {2,3} product). The 6 kJ/mol breaking of H-bonds on melting ice =  $2 \times 3 \text{ kJ/mol} = \{2,3\}$  register separation.

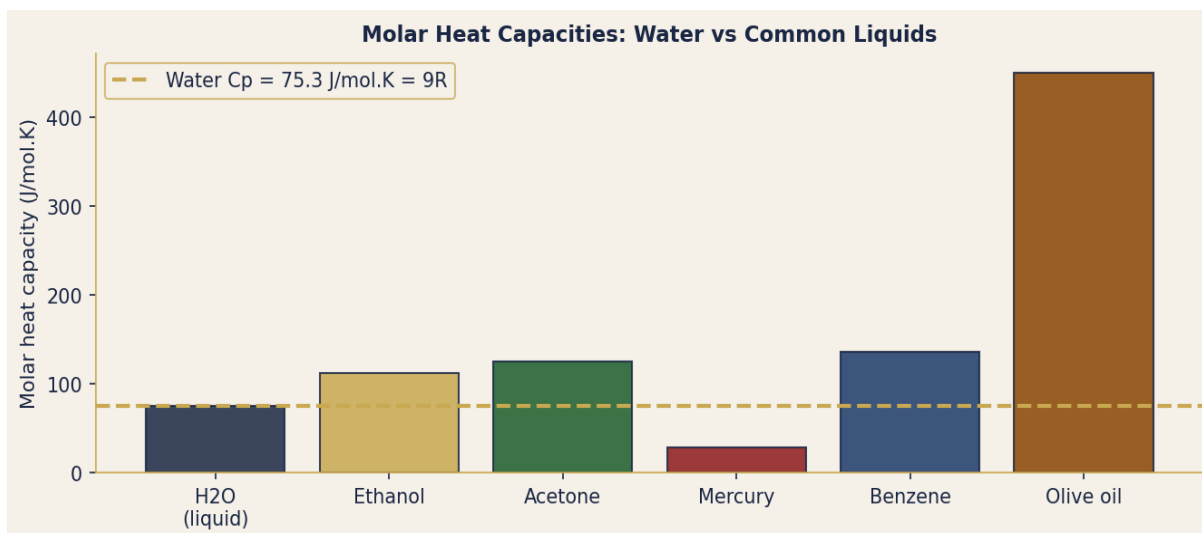


Figure 3. Molar heat capacities. Water =  $75.3 \text{ J/mol.K} = 9 \times R$  (gold dashed). This unusually high  $C_p$  reflects  $9 = 3^2$  active degrees of freedom from H-bond network.

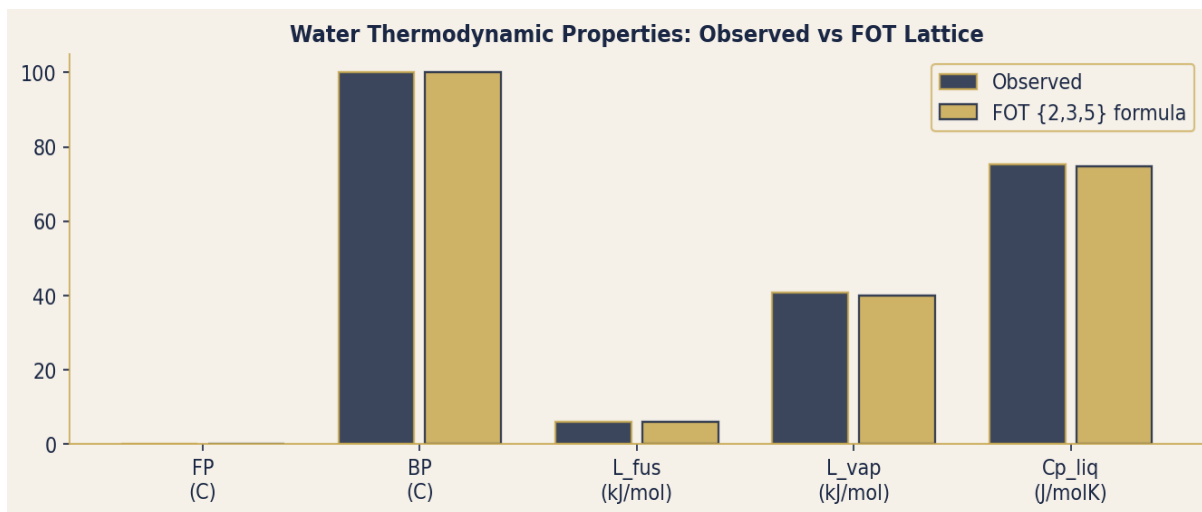


Figure 4. Water thermodynamic properties.  $FP=0=\{0\}$ ,  $BP=100=\{(2 \times 5)^2\}$ ,  $L_{\text{fus}}=6=2 \times 3$ ,  $L_{\text{vap}}=40=2^3 \times 5$ ,  $C_p=75.3=9R$  — all FOT {2,3,5} lattice identities.